

Police DAV Public School, Ludhiana
Class –XII/ Mathematics

- Q.1 If A is square matrix of order $n \times n$ then $\text{adj}(\text{adj} A)$ is equal to
 (a) $|A|^n A$ (b) $|A|^{n-1} A$ (c) $|A|^{n-2} A$ (d) $|A|^{n-3} A$
- Q.2 If A is an orthogonal matrix, then A^{-1} equals
 (a) A (b) A^T (c) A^2 (d) I
- Q.3 If $A = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$, then $\lim_{n \rightarrow \infty} \frac{A^n}{n}$ is
 (a) Zero matrix (b) Identity matrix (c) $\begin{pmatrix} 0 & 1 \\ 0 & -1 \end{pmatrix}$ (d) $\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$
- Q.4 The value of a 3×3 determinant is 11, then the value of determinant formed by its cofactors will be
 (a) 11 (b) 121 (c) 1331 (d) 14641
- Q.5 $f(x) = \begin{vmatrix} \cos x & x & 1 \\ 2\sin x & x^2 & 2x \\ \tan x & x & 1 \end{vmatrix}$, then $\lim_{x \rightarrow 0} \left[\frac{f'(x)}{x} \right]$
 (a) 2 (b) -2 (c) 1 (d) -1
- Q.6 If $a^2 + b^2 + c^2 = -2$ and
 $f(x) = \begin{vmatrix} 1+a^2x & (1+b^2)x & (1+c^2)x \\ (1+a^2)x & 1+b^2x & (1+c^2)x \\ (1+a^2)x & (1+b^2)x & 1+c^2x \end{vmatrix}$
 Then $f(x)$ is a polynomial of degree
 (a) 0 (b) 1 (c) 2 (d) 3
- Q.7 Let f be a function satisfying $f(x+y) = f(x)f(y) \forall x \in R$. If $f(1) = 3$ then $\sum_{r=1}^n f(r)$ is equal to
 (a) $\frac{3}{2}(3^n - 1)$ (b) $\frac{3}{2}n(n+1)$ (c) $3^{n+1} - 3$ (d) $\frac{3}{2}(3^n + 1)$
- Q.8 $f(x) = \lim_{t \rightarrow \infty} \frac{(1 + \sin \pi x)^t - 1}{(1 + \sin \pi x)^t + 1}$, then range of $f(x)$ is
 (a) (-1, 1) (b) (0, 1) (c) (-1, 0) (d) (-1, 0, 1)
- Q.9 If $f(x) = \frac{4^x}{4^x + 2}$, then $f\left(\frac{1}{1997}\right) + f\left(\frac{2}{1997}\right) + f\left(\frac{3}{1997}\right) + \dots + f\left(\frac{1996}{1997}\right)$ is equal to
 (a) 1997 (b) 998 (c) 0 (d) 997

Q.10 The set of points of discontinuity of $f(x) = \lim_{x \rightarrow \infty} \frac{x^{-n} - x^n}{x^{-n} + x^n}$ is

- (a) $\{1\}$ (b) $\{-1\}$ (c) $\{-1,1\}$ (d) $\{0\}$

Q.11 Let f be a differentiable function such that $f\left(\frac{x}{y}\right) = \frac{f(x)}{f(y)}$ for all $x, y \in \mathbb{R}, y \neq 0$. If $f'(1)=2$, then $f'(x)$ is equal to

- (a) $2f(x)$ (b) $\frac{f(x)}{x}$ (c) $2xf(x)$ (d) $\frac{2f(x)}{x}$

Q.12 $\frac{d}{dx} \cos(\sin x^2)$, at $x = \sqrt{\sqrt{\pi}/2}$ is

- (a) -1 (b) 1 (c) 2 (d) 0

Q.13 $y \cos x + x \cos y = \pi$, then $y''(0)$ is

- (a) 1 (b) π (c) 0 (d) $-\pi$

Q.14 $f(x) = (1+x)^n$, then value of $f(x) = f(0) + \frac{f'(0)}{1!}x + \frac{f''(0)}{2!}x^2 + \frac{f'''(0)}{3!}x^3 + \dots + \frac{f^{(n)}(0)}{n!}x^n$ is

- (a) n (b) 2^n (c) 2^{n-1} (d) 2^{n-2}

Q.15 If $f(x) = x + \tan x$, f is inverse of g , then $g(x)$ is equal to

- (a) $\frac{1}{1+(g(x)-x)^2}$ (b) $\frac{1}{1-(g(x)-x)^2}$
 (c) $\frac{1}{2+(g(x)-x)^2}$ (d) $\frac{1}{2-(g(x)-x)^2}$

Q.16 Range of $f(x) = \sin^{-1} x + \tan^{-1} x + \sec^{-1} x$ is

- (a) $\left[\frac{\pi}{4}, \frac{3\pi}{4} \right]$ (b) $\left[\frac{\pi}{4}, \frac{3\pi}{4} \right)$
 (c) $\left[\frac{\pi}{4}, \frac{3\pi}{4} \right)$ (d) $\left[\frac{\pi}{4}, \frac{3\pi}{4} \right]$

Q.17 If $x^2 + y^2 + z^2 = r^2$, the $\tan^{-1}\left(\frac{xy}{zr}\right) + \tan^{-1}\left(\frac{yz}{xr}\right) + \tan^{-1}\left(\frac{zx}{yr}\right)$ is

- (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{2}$ (c) 0 (d) $-\frac{\pi}{2}$

Q.18 Sum of series $\cot^{-1}(2) + \cot^{-1}(8) + \cot^{-1}(18) + \cot^{-1}(32) \dots$ upto ∞ is equal to

- (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{2}$ (c) $\frac{\pi}{4}$ (d) 0

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Class –XII/Mathematics

Q.1 Consider $f: \mathbb{R}_+ \rightarrow \{-9, \infty\}$ given by $f(x) = 5x^2 + 6x - 9$. Prove that f is invertible with $f^{-1}(y) = \left\{ \frac{\sqrt{54+5y-3}}{5} \right\}$

Q.2 If $f: \mathbb{N} \rightarrow \mathbb{N}$ is defined by

$$f(n) = \begin{cases} \frac{n+1}{2}, & \text{if } n \text{ is odd} \\ \frac{n}{2}, & \text{if } n \text{ is even} \end{cases} \quad \text{for all } n \in \mathbb{N}$$

Find whether the function f is bijective.

Q.3 Express the following matrix as a sum of a symmetric and a skew-symmetric matrices and verify your result.

$$\begin{pmatrix} 3 & -2 & -4 \\ 3 & -2 & -5 \\ -1 & 1 & 2 \end{pmatrix}$$

Q.4 Find inverse using elementary transformation.

$$\begin{pmatrix} -1 & 3 & 0 \\ 0 & -2 & 1 \end{pmatrix}$$

Q.5 Using properties of determinants, prove that

$$\begin{vmatrix} x^2+1 & xy & xz \\ xy & y^2+1 & yz \\ xz & yz & z^2+1 \end{vmatrix} = 1 + x^2 + y^2 + z^2$$

Q.6 If $A = \begin{pmatrix} 1 & -2 & 0 \\ 2 & 1 & 3 \\ 0 & -2 & 1 \end{pmatrix}$ and $B = \begin{pmatrix} 7 & 2 & -6 \\ -2 & 1 & -3 \\ -4 & 2 & 5 \end{pmatrix}$

Find AB and hence solve system of equations $x - 2y = 10$, $2x + y + 3z = 8$, $-2y + z = 7$.

Q.7 If $A = \begin{pmatrix} 1 & -1 & 0 \\ 2 & 3 & 4 \\ 0 & 1 & 2 \end{pmatrix}$ and $B = \begin{pmatrix} 2 & 2 & -4 \\ -4 & 2 & -4 \\ 2 & -1 & 5 \end{pmatrix}$

Then find AB . Use this to solve this system of equations: $x - y = 3$, $2x + 3y + 4z = 17$, $y + 2z = 7$.

Q.8 $f(x) = \begin{cases} \frac{1-\cos 4x}{x^2}, & \text{when } x < 0 \\ a, & \text{when } x = 0 \\ \frac{\sqrt{x}}{\sqrt{16 - \sqrt{x}} - 4}, & \text{when } x > 0 \end{cases}$

and f is continuous at $x = 0$, then find the value of a .

Q.9 Find the value of k, for which

$$f(x) \begin{cases} \frac{\sqrt{1+kx} - \sqrt{1-kx}}{x} & \text{if } -1 \leq x < 0 \\ \frac{2x+1}{x-1} & \text{if } 0 \leq x < 1 \end{cases}$$

is continuous at $x = 0$.

Q.10 If $e^x + e^y = e^{x+y}$, prove that $\frac{dy}{dx} + e^{y-x} = 0$

Q.11 Differentiate $\tan^{-1}\left(\frac{\sqrt{1-x^2}}{x}\right)$ w.r.t $\cos^{-1}(2x\sqrt{1-x^2})$, when $x \neq 0$

Q.12 Differentiate the following with respect to x

$$\sin^{-1}\left(\frac{2^{x+1} \cdot 3^x}{1+(36)^x}\right)$$

Q.13 If $(\cos x)^y = (\cos y)^x$, the find $\frac{dy}{dx}$

Q.14 If $\sin y = x \sin(a+y)$, then prove that $\frac{dy}{dx} = \frac{\sin^2(a+y)}{\sin a}$

Q.15 If $(\tan^{-1}x)^y + y^{\cot x} = 1$, then find dy/dx .

Q.16 Find the intervals in which the function given by $f(x) = \sin x + \cos x$, $0 \leq x \leq 2\pi$ is
(i) increasing (ii) decreasing

Q.17 Find the point on the curve $9y^2 = x^3$, where the normal to the curve makes equal intercepts on the axes.

Q.18 Find the equations of tangents to the curve $3x^2 - y^2 = 8$, which passes through the point $\left(\frac{4}{3}, 0\right)$

Q.19 Show that the semi-vertical angle of the cone of the maximum volume and of given slant height is $\cos^{-1} \frac{1}{\sqrt{3}}$.

Q.20 Show that of all the rectangles of given area, the square has the smallest perimeter.

Q.21 AB is diameter of a circle and C is any point on the circle. Show that the area of ΔABC is maximum when it is isosceles.